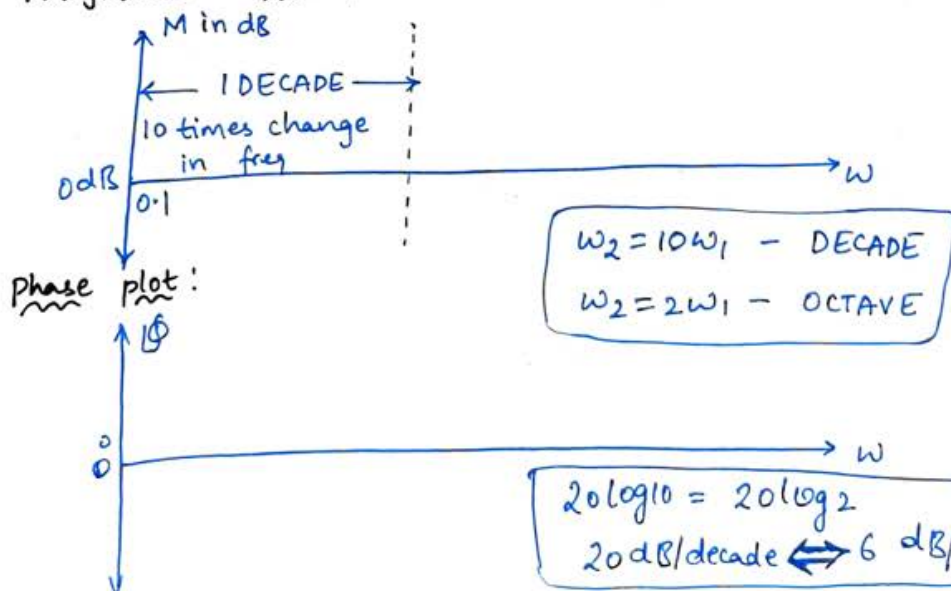


BODE PLOTS :

Purpose:

1. To draw the freq. response of OLTF
2. To find the closed loop system stability.
3. To find the gain margin and phase margin, gain cross-over frequency (ω_{gc}), phase cross over frequency (ω_{pc}).
4. To find the relative stability by using gain margin and phase margin.
5. If the gain margin & phase margin is very large then the system is more relatively stable but the system response become slow.
6. If the gain margin & phase margin is very small then the system is less relatively stable and more oscillatory.
7. The optimum range of gain margin is (5dB - 10dB)
8. The optimum range of phase margin is (30° - 40°)
9. The bode plot consists the two plots
 - (i) Magnitude plot
 - (ii) Phase plot

Magnitude plot:



Phase plot:

Diagram illustrating the Phase plot. The vertical axis is labeled ϕ and the horizontal axis is labeled ω . A horizontal line is drawn at 0° .

$$20 \log 10 = 20 \log 2$$
$$20 \text{ dB/decade} \Leftrightarrow 6 \text{ dB/octave}$$

Procedure to draw bode plot:

1. Replace s by $j\omega$ to convert into freq. domain.
2. Write the magnitude and convert into decibels. The magnitude in dB is

$$M_{\text{indB}} = 20 \log |GH(j\omega)|.$$

3. Write the phase angle by using $\tan^{-1} \left(\frac{\text{Im part}}{\text{Real part}} \right)$.

$$\phi = \tan^{-1} \left(\frac{I.P}{R.P} \right)$$

4. Vary the ' ω ' from minimum to maximum and draw the approximated magnitude & phase plot.

Q. Draw the bode plot of $G(s)H(s) = K$.

Sol. Procedure:

$$s \rightarrow j\omega.$$

$$GH(j\omega) = K.$$

$$M = K.$$

$$M_{\text{indB}} = 20 \log K = \text{Magnitude}$$

$$\text{Slope} = \frac{dM}{d \log \omega} = 0 \text{ dB/decade}.$$

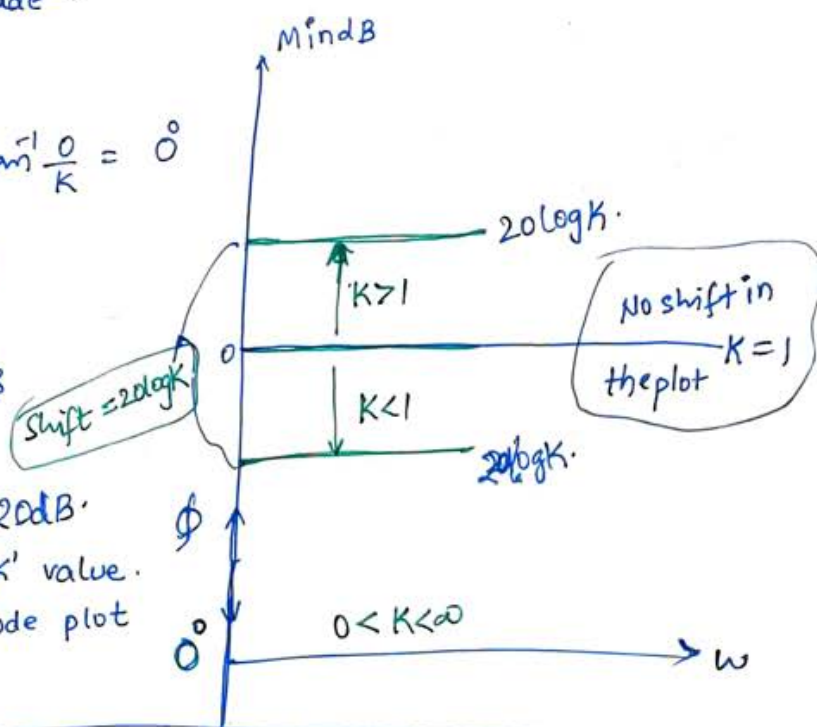
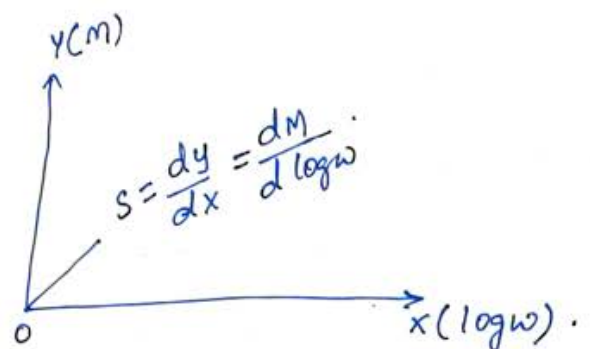
$$\text{phase} = \angle \phi = \angle (K + j0) = \tan^{-1} \frac{0}{K} = 0^\circ$$

$$\text{if } K=1 \rightarrow M_{\text{indB}} = 0 \text{ dB}$$

$$\text{if } K=10 (>1) \rightarrow M_{\text{indB}} = 20 \text{ dB}$$

$$\text{if } K=0.1 (<1) \rightarrow M_{\text{indB}} = -20 \text{ dB}.$$

→ The phase plot is independent of 'K' value. Whereas the shift in the magnitude plot depends on 'K' value



'Poles' at origin: $\rightarrow S \sim -20n \text{ dB/dec}$
 $\phi = -90^\circ n$

$$G(s)H(s) = \frac{1}{s^n}$$

$$s \rightarrow j\omega$$

$$G_H(j\omega) = \frac{1}{(j\omega)^n}$$

$$M = \frac{1}{\omega^n} ; \text{ slope } S = \frac{dM}{d \log \omega}$$

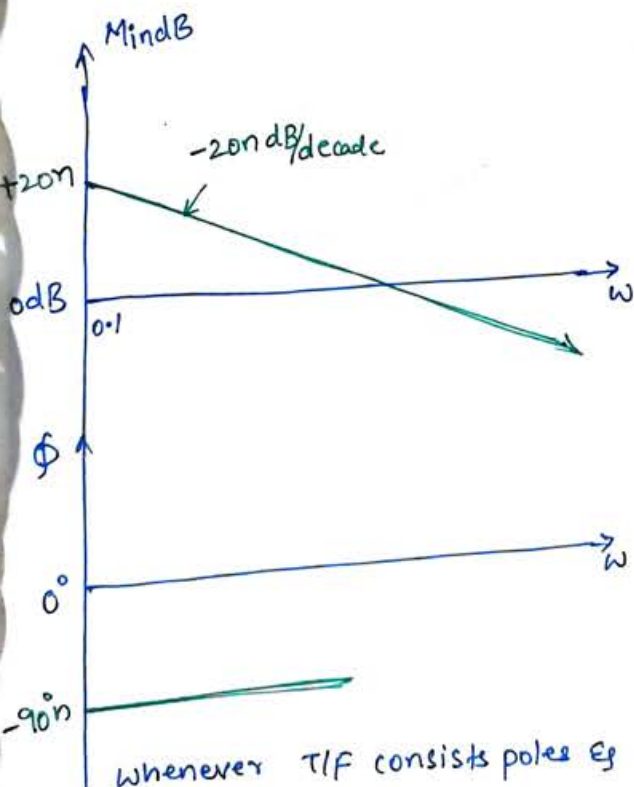
$$S \approx M_{\text{in dB}} = -20n \log \omega \text{ dB}$$

$$S = \frac{dM}{d \log \omega} = -20n \text{ dB/decade}$$

$$\phi = \frac{\angle 1}{\angle j\omega \dots n \text{ times}} = \frac{0^\circ}{90^\circ n} = -90^\circ n$$

$$M|_{\omega=0.1} = -\text{slope}$$

$$M|_{\omega=1} = 0 \text{ dB}$$



Whenever T/F consists poles & zeros at origin, then the plot should start with a magnitude of opposite sign of slope at a freq of 0.1 & should

'Zeros' at origin:

$$G_H(s) = s^n$$

$$s \rightarrow j\omega$$

$$G_H(j\omega) = (j\omega)^n$$

$$M = \omega^n ; \text{ slope } S = \frac{dM}{d \log \omega}$$

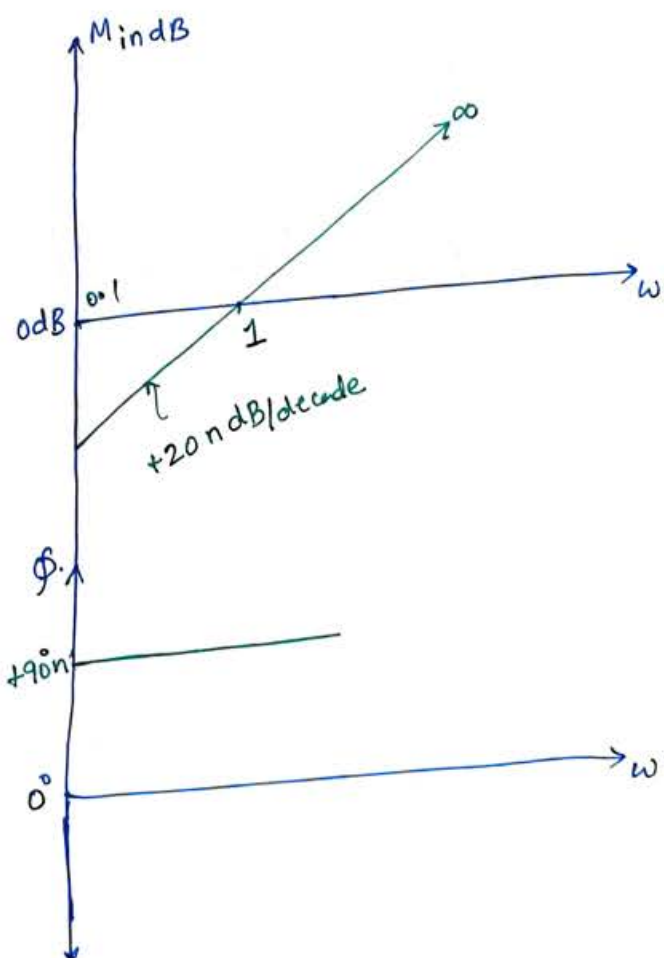
$$M_{\text{in dB}} = +20n \log \omega \text{ dB}$$

$$S = \frac{dM}{d \log \omega} = 20n$$

$$\phi = \angle j\omega \dots n \text{ times} = +90^\circ n$$

$$M|_{\omega=0.1} = -\text{slope}$$

$$M|_{\omega=1} = 0 \text{ dB}$$



pass through 0 dB line intersect 0 dB at $\omega=1$ & extended upto ∞ if no corner frequency existed.

④ Draw the bode plot. $G_H(s) = \frac{100}{s^8}$.

Sol. $G_H(s) = \frac{100}{s^8}$; $s \rightarrow j\omega$; $\Rightarrow G_H(j\omega) = \frac{100}{(j\omega)^8}$.

$M = \frac{100}{\omega^8}$; $M_{\text{indB}} = +20 \log \frac{100}{\omega^8} = +20 \log 100 - 20 \times 8 \log \omega$

Do not use the procedure even though you get answer. Use the analysis we have done already.

i.e., 8 poles at origin ; Slope $S = -20 \times 8 = -160 \text{ dB/decade}$.

Phase $\phi = -90^\circ \times 8 = -720^\circ$

Shift $= 20 \log 100 = +40 \text{ dB}$.

